Mid Term Exam (MTE) will be held on 28-th of October, at 17:30 by Zoom.

Please participate with your own computers with installed Octave and my .m files.

During the MTE you must solve 2 problems:

- 1. Diffie-Hellman Key Agreement Protocol DH KAP.
- 2. Man-in-the-Middle Attack (MiMA) for Diffie-Hellman Key Agreement Protocol DH KAP.

The problems are presented in the site:

imimsociety.net

In section 'Cryptography':

Cryptography (imimsociety.net)

Please register to the site and after that you receive 10 Eur virtual money to purchase the problems. For registration you should input the first 2 letters of your Surname and full Name, e.g. John Smith Should register as **Sm John**.

Please purchase the only one problem at a time.

If the solution is successful then you are invited to press the green button [Get reward].

No any other declaration about the solution results is required.

If the solution failed, then you must press the button [Return] in the top on the left side.

Then 'Knowledge bank' will pay you the sum twice you have paid.

So, if the initial capital was 10 Eur of virtual money and you buy the problem of 2 Eur, then if the solution is correct your budget will increase up to 12 Eur.

You can solve the problems in imimsociety as many times as you wish to better prepare for MTE.

I advise you to try at first to solve the problem in 'Intellect' section to exercise the brains.

It is named as 'WOLF, GOAT AND CABBAGE TRANSFER ACROSS THE RIVER ALGORITHM'.

< https://imimsociety.net/en/home/15-wolf-goat-and-cabbage-transfer-across-the-river-algorithm.html>







WOLF, GOAT AND CABBAGE

€2.00

Cryptography: information

confidentiality, integrity, authenticity, person identification

Symmetric cryptography ------ Asymmetric cryptography 1976

Asymmetric encryption

Symmetric encryption.

Symmetric encryption:

block ciphers stream ciphers

H-functions, Message digest
HMAC H-Message Authentication Code

Asymmetric encryption

E-signature - Public Key Infrastructure - PKI Blockchain, Cryptocurrecy, E-money

E-voting

Digital Rights Management - DRM (Marlin) Etc.

A **cryptographic hash function** is a special class of <u>hash function</u> that has certain properties which make it suitable for use in <u>cryptography</u>. It is a mathematical <u>algorithm</u> that <u>maps</u> data of arbitrary finite size to a <u>bit string</u> of a fixed size (a <u>hash function</u>) which is designed to also be a <u>one-way function</u>, that is, a function which is infeasible to invert.

The only way to recreate the input data from an ideal cryptographic hash function's output is to attempt a <u>brute-force search</u> of possible inputs to see if they produce a match.

The input data is often called the *message*, and the output (the *hash* value or hash) is often called the *message digest* or simply the *digest*.

From https://en.wikipedia.org/wiki/Cryptographic hash function

$$M - message$$
 $h = H(M)$
 $|h| = 256 \text{ bits}$
 $|h| = 28 \text{ bits}$
 $= 7 \text{ hex numb.}$
 $|h| = 000 = 000$

$$0000_{b} = O_{h} = O_{d}$$

$$0001_{b} = 1_{h} = 1_{d}$$

$$0010_{b} = 2_{h} = 2_{d}$$

$$1001_{b} = 9_{10}$$

$$1010_{b} = A_{h} = 10_{10}$$

$$1110_{b} = E_{h} = 14_{10}$$

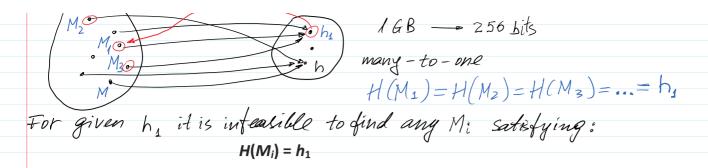
$$1111_{b} = F_{h} = 15_{10}$$

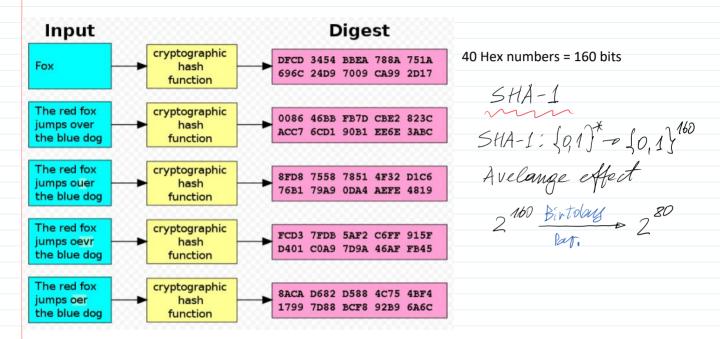
Cryptographic hash functions have many <u>information-security</u> applications, notably in <u>digital signatures</u>, <u>message authentication codes</u> (HMACs), and other forms of <u>authentication</u>. They can also be used as ordinary <u>hash functions</u>, to index data in <u>hash tables</u>, for <u>fingerprinting</u>, to detect duplicate data or uniquely identify files, and as <u>checksums</u> to detect accidental data corruption. Indeed, in information-security contexts, cryptographic hash values are sometimes called (*digital*) *fingerprints*, *message digest* or just *hash values*, even though all these terms stand for more general functions with rather different properties and purposes.

$$M - message : H(M) = h$$
 $M \in \{0,1\}^* : h \in \{0,1\}^{256} : H : \{0,1\}^* \rightarrow \{0,1\}^{256} / SHA256$

Preimage Smage

 $M_2^{O} \longrightarrow M_3^{O} \longrightarrow M_3$





A cryptographic hash function (specifically <u>SHA-1</u>) at work. A small change in the input (in the word "over") drastically changes the output (digest). This is the so-called <u>avalanche effect</u>.

Properties

- It is quick to compute the hash value for any given finite message.
- A small change to a message should change the hash value so extensively that the new hash value appears uncorrelated with the old hash value.
- Security properties presented below.

Most cryptographic hash functions are designed to take a <u>string</u> of any finite length as input and produce a fixed-length hash value.

A cryptographic hash function must be able to withstand all known types of cryptanalytic attack. In theoretical cryptography, the security level of a cryptographic hash function has been defined using the following properties:

Pre-image resistance

Given a hash value h it should be difficult to find any message M such that h = H(M). This concept is related to that of <u>one-way function</u>. Functions that lack this property are vulnerable to first preimage attacks.

• Second pre-image resistance

Given an input M_1 it should be difficult to find (different) input M_2 such that $H(M_1) = H(M_2)$. Functions that lack this property are vulnerable to second-preimage attacks.

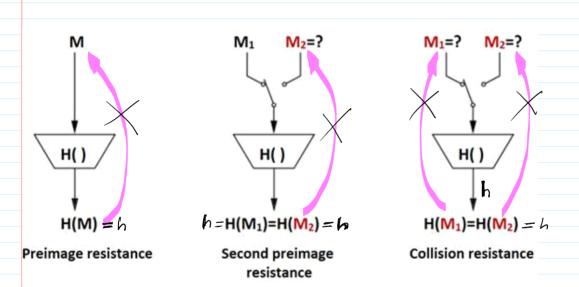
• Collision resistance

It should be difficult to find any two different messages M_1 and M_2 such that $H(M_1) = M(M_2)$. Such a pair is called a cryptographic <u>hash collision</u>. This property is sometimes referred to as *strong collision resistance*. It requires a hash value at least twice as long as that required for preimage-resistance; otherwise **collisions** may be found by a <u>birthday attack</u>. [2] These properties form a hierarchy, in that collision resistance implies second pre-image resistance, which in turns implies pre-image resistance, while the converse is not true in general. [3]

The weaker assumption is always preferred in theoretical cryptography, but in practice, a hash-functions which is only second pre-image resistant is considered insecure and is therefore not recommended for real applications.

Informally, these properties mean that a <u>malicious adversary</u> cannot replace or modify the input data without changing its digest.

Thus, if two strings have the same digest, one can be very confident that they are identical.



Loan contract

$$M_1 = 1000 \in loan$$
. $M_1 - is a valid loan contract$.
 $h = H(M_1); |h| = 256 \text{ bits}$
 $A: PrK_A = X \longrightarrow Sign(PrK_A, h) = G_n = (r_A, s_A)$
 $M_1, G_h, PuK_A \longrightarrow J_0: Jinds second preimage M_2
to create loan contract for $100000 \in such that H(M_1) = H(M_2) = h$$

Then the valid signature on M1 is valid also on M2.

A:
$$h = H(M_2) \Rightarrow M_2$$
, G_h claim to Alice to pay

11. (G. h . $R_1 K_1$) = True 100 000 ϵ (instead of 1000 ϵ)

$$f: h = H(M_2) \Rightarrow M_2, 6h$$
 claim to Alice to pay
 $Ver(6h, h, PuK_A) = True$ 100 000 \in (instead of 1000 \in)

hd28.m - computing 28 bit length h-value in decimal form h28.m - computing 28 bit length h-value in hexadecimal form sha256.m - computing 256 bit length h-value in hexadecimal form

>> sha256('RootHash PrevHash 737327631')

ans = F4AE534CD226FAF7998C8424B348E020BA80639A687E93A0B8C5130EDC51E6DE

>> h28('RootHash PrevHash 737327631')

ans = C51E6DE

>> hd28('RootHash PrevHash 737327631')

ans = 206694110

>> dec2bin(ans)

ans = 1100010100011110011011011110

>> dec2hex(206694110)

ans = C51E6DE

Illustration

nonce = 737327631

>> sha256('RootHash PrevHash 737327631')

ans = F4AE534CD226FAF799 8C8424B348E020BA80639A687E93A0B8C5130ED C51E6DE

>> sha256('RootHash PrevHash 737327632')

ans = B856211DF2EE15E30AB770C1A43CE014ECFE573182AFD885B28D96854DBC5F21

>> sha256('RootHash PrevHash 737327633')

ans = 9C18C764E347A58E57AC3F7A3C2874D5889A0E802699FEA47EEFF8C03BFEDA69

>> sha256('RootHash PrevHash 737327634')

ans = 32B2108A70C39565485CCED9C948E5B7A0027D1EE98642E09D5E4D3D84E16814

>> sha256('RootHash PrevHash 737327635')

ans = $\frac{A}{2}$ 281AC77F5C9AEDEEFFDEDEA85DCEA1C5D76E4222AB80D8A456AEB2AA9EB0F44

$$O_{h} = 0000_{2} \; j \; F_{h} = 1111_{2}$$

h28(°---°) → 7 hex numb. hd28(°---°) → decimal num.

Commitment

An illustration of the potential use of a cryptographic hash is as follows: Alice poses a tough math problem to Bob and claims she has solved it. Bob would like to try it himself, but would yet like to be sure that Alice is not bluffing.

Therefore, Alice writes down her solution, computes its hash and tells Bob the hash value (whilst keeping the solution secret).

Then, when Bob comes up with the solution himself a few days later, Alice can prove that she had the solution earlier by revealing it and having Bob hash it and check that it matches the hash value given to him before. (This is an example of a simple commitment scheme; in actual practice, Alice and Bob will often be

P= NP P = NP

computer programs, and the secret would be something less easily spoofed than a claimed puzzle solution).

Verifying the integrity of files or messages

Main article: File verification

An important application of secure hashes is verification of message integrity. Determining whether any changes have been made to a message (or a file), for example, can be accomplished by comparing message digests calculated before, and after, transmission (or any other event).

For this reason, most <u>digital signature</u> algorithms only confirm the authenticity of a hashed digest of the message to be "signed". Verifying the authenticity of a hashed digest of the message is considered proof that the message itself is authentic.

MD5, SHA1, or SHA2 hashes are sometimes posted along with files on websites or forums to allow verification of integrity. [6] This practice establishes a chain of trust so long as the hashes are posted on a site authenticated by HTTPS.

Password verification[edit]

Main article: password hashing

A related application is <u>password</u> verification (first invented by <u>Roger Needham</u>). Storing all user passwords as <u>cleartext</u> can result in a massive security breach if the password file is compromised. One way to reduce this danger is to only store the hash digest of each password. To authenticate a user, the password presented by the user is hashed and compared with the stored hash. (Note that this approach prevents the original passwords from being retrieved if forgotten or lost, and they have to be replaced with new ones.) **The password is often concatenated with a random, non-secret <u>salt value</u> before the hash function is applied. The salt is stored with the password hash. Because users have different salts, it is not feasible to store tables of <u>precomputed</u> hash values for common passwords. <u>Key stretching</u> functions, such as <u>PBKDF2</u>, <u>Bcrypt</u> or <u>Scrypt</u>, typically use repeated invocations of a cryptographic hash to increase the time required to perform <u>brute force attacks</u> on stored password digests.

In 2013 a long-term <u>Password Hashing Competition</u> was announced to choose a**

In 2013 a long-term Password Hashing Competition was announced to choose a new, standard algorithm for password hashing.

Proof-of-work

Main article: Proof-of-work system

A proof-of-work system (or protocol, or function) is an *economic* measure to deter <u>denial of service</u> attacks and other service abuses such as spam on a network by requiring some work from the service requester, usually meaning processing time by a computer. A key feature of these schemes is their asymmetry: the work must be moderately hard (but feasible) on the requester side but easy to check for the service provider.

One popular system — used in <u>Bitcoin mining</u> and <u>Hashcash</u> — **uses partial hash inversions to prove that work was done,** as a good-will token to send an e-mail. The sender is required to find a message whose hash value begins with a number of zero bits. The average work that sender needs to perform in order to find a valid message is

L. f * f'
H(f) * H(f')
h h'
Sign (Prk, h) * Sign (Prk,h')

inversions to prove that work was done, as a good-will token to send an e-mail. The sender is required to find a message whose hash value begins with a number of zero bits. The average work that sender needs to perform in order to find a valid message is exponential in the number of zero bits required in the hash value, while the recipient can verify the validity of the message by executing a single hash function. For instance, in Hashcash, a sender is asked to generate a header whose 160 bit SHA-1 hash value has the first 20 bits as zeros. The sender will *on average* have to try 2¹⁹ times to find a valid header.

202 = 1M

File or data identifier

A message digest can also serve as a means of reliably identifying a file; several <u>source code management</u> systems, including <u>Git</u>, <u>Mercurial</u> and <u>Monotone</u>, use the <u>sha1sum</u> of various types of content (file content, directory trees, ancestry information, etc.) to uniquely identify them. Hashes are used to identify files on peer-to-peer filesharing networks.

Pseudorandom generation and key derivation

Hash functions can also be used in the generation of <u>pseudorandom</u> bits, or to derive new keys or passwords from a single secure key or password.

As of 2009, the two most commonly used cryptographic hash functions were MD5 and SHA-1. However, a successful attack on MD5 broke Transport Layer Security in 2008.

In February 2005, an attack on SHA-1 was reported that would find collision in about 2⁶⁹ hashing operations, rather than the 2⁸⁰ expected for a 160-bit hash function. In August 2005, another attack on SHA-1 was reported that would find collisions in 2⁶³ operations. Though theoretical weaknesses of SHA-1 exist, [14][15] no collision (or near-collision) has yet been found. Nonetheless, it is often suggested that it may be practical to break within years, and that new applications can avoid these problems by using later members of the SHA family, such as SHA-2.

According to birthday paradox it is not required total scan all 2^{160} variants of message M. It is enough to scan $\sqrt{2^{160}} = 2^{80}$ variants.

SHA-2 (Secure Hash Algorithm 2) is a set of <u>cryptographic hash</u>
<u>functions</u> designed by the United States <u>National Security Agency</u> (NSA).

From https://en.wikipedia.org/wiki/SHA-2

SHA-2 includes significant changes from its predecessor, <u>SHA-1</u>.
The SHA-2 family consists of six hash functions with <u>digests</u> (hash values) that are 224, 256, 384 or 512 bits:

h28

SHA-224, <mark>SHA-256</mark>, SHA-384, <mark>SHA-512</mark>, SHA-512/224, SHA-512/256.

However, to ensure the long-term robustness of applications that use hash functions, there was a competition to design a replacement for SHA-2.

On October 2, 2012, Keccak was selected as the winner of the <u>NIST</u> hash function competition.

A version of this algorithm became a FIPS standard on August 5, 2015 under the name SHA-3 <--> keccak-256 --> in Ethereum

HMAC - H Message Authentication Code

Use in building other cryptographic primitives: symmetric e-signature realization

Hash functions can be used to build other cryptographic primitives.

For these other primitives to be cryptographically secure, care must be taken to build them correctly.

Message authentication codes (MACs) (also called keyed hash functions) are often built from hash functions. HMAC is such a MAC.

Information confidentiality

Authentication

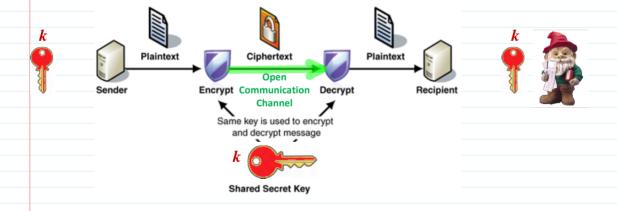
Integrity

Keyed-hash message authentication code (**HMAC**) is a specific type of message authentication code (MAC) involving a cryptographic hash function (hence the 'H') in combination with a secret cryptographic key. As with any MAC, it may be used to simultaneously verify both the data integrity and the authentication of a message.

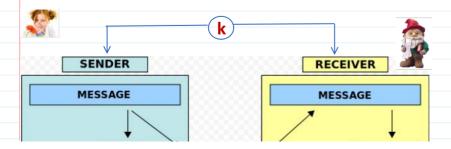
Any cryptographic hash function, may be used in the calculation of an HMAC.

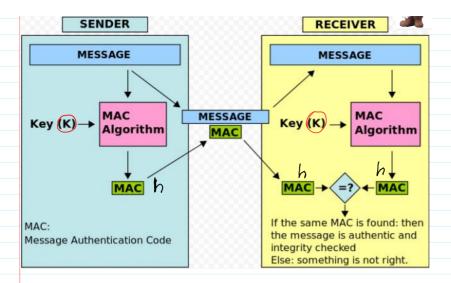
The cryptographic strength of the HMAC depends upon the <u>cryptographic strength</u> of the underlying hash function, the size of its hash output, and on the size and quality of the key.

Symmetric - Secret Key Encryption - Decryption

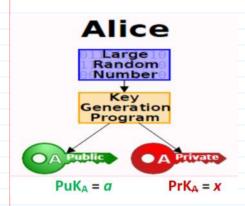


Integrity and authenticity by computing h-value and signing HMAC based symmetric e-signature





Asymmetric cryptography

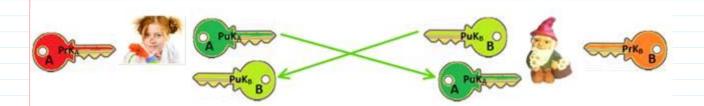


 $\mathbf{PP} = (\boldsymbol{p}, \boldsymbol{g}).$

Strong prime number p in real cryptography is of order: $p \sim 2^{2048}$ Strong prime number p in our examples is of order: $p \sim 2^{28}$ >> p=genstrongprime(28)

Key generation

- Randomly choose a private key X with 1 < x < p 1.
- The private key is PrK = x = randi(p-1)Compute $a = g^x \mod p$.
- The public key is $PuK = a = q^x \mod p$.

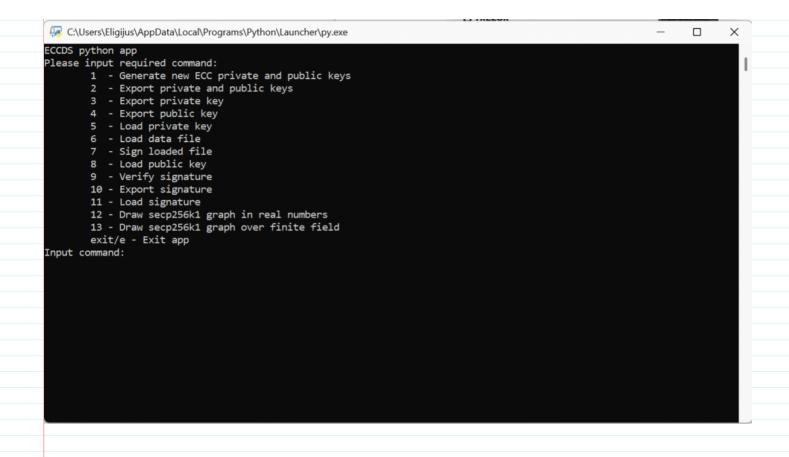


<u>Trezor Hardware Wallet (Official) | Bitcoin & Crypto Security</u>

The safest cold storage wallets for crypt security and financial independence. Easily use, store, and protect Bitcoins. trezor.io

Secure coins with Trezor

C:\Users\Eligijus\Documents\500 SOFTAS App 2023\Python 3.9.1\111.ECDSA-secp256k1 Python.Edv.Rep\ECC



Till this place

Confidentiality, Integrity and Authenticity by encryption, computing h-value and signing

A; message M to be sent to B.

1. Parties agree on the common secret Key k.

2. A encrypts message using symmetric encryption algorithm, e.g. AES128: C = AES(k, M); $|C| \approx |M|$.

3. The HMAC-value on G is computed: h = HMAC(k, G)

 $\rightarrow \mathcal{B}$:
1. Computes HMAC-value on G h' = HMAC(k, G)

2. Verifies received h-value h
with computed h

$$Ver(If h = h') = \{ \uparrow, \mid \}$$

Ver
$$(I \mid h = h') = \{\uparrow, \downarrow \}$$

3. Decrypts G by k
 $D(k, G) = M$.

In the case of Asymmetric cryptography: Confidentiality Integrity and Authenticity is realized by encryption, computing h-value and signing

A; message M to be sent to B.

- 1. Porties agree on the common secret Key K.
- 2. A encrypts message using symmetric encryption algorithm, e.g. AES128: C = AES(k, M); |C| ~ |M|.
- 3. The h-value of G is computed: h = sha256 (G)
- 4. The signature is placed on h: Sign(PrkA, h) = 8 = (r, s)

A: PrKA=X; PuKA=a.

 $\mathcal{B}: PK_B = Y; PuK_B = b.$ $\mathcal{C}, \ \mathcal{C} = (r, s) \qquad PuK_A = a.$

- 1. Computes b value of G h = sha256(G)
- 2. Verifies signature on h $Ver(Puk_A, 6, h) = 17, F$
- 3. Decrypts G by k D(k, G) = M.

Telecommunik

$$K_{A1}$$

$$K_{B2}$$

$$K_{B1}$$

$$K_{A2}$$

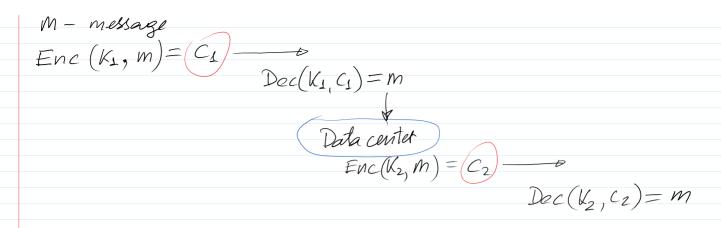
$$K_{B2}$$

$$K_{AB} = (K_B)^{\times} \mod p \qquad K \qquad (K_A)^{Y} \mod p - K_{BA}$$

$$K_{AB} = (K_A)^{X} \mod p - K_{BA}$$

$$K_{AB} = (K_A)^{X} \mod p - K_{BA}$$

$$K_{AB} = (K_B)^{\times} \mod p - K_{BA}$$



software and its Telecommunik

>> sha256('RootHash PrevHash 737327631')

ans = F4AE534CD226FAF7998C8424B348E020BA80639A687E93A0B8C5130EDC51E6DE

>> h28('RootHash PrevHash 737327631')

ans = C51E6DE

>> hd28('RootHash PrevHash 737327631')

ans = 206694110

>> dec2bin(ans)

ans = 1100010100011110011011011110

>> dec2hex(206694110)

ans = C51E6DE

Hash functions based on block ciphers

There are several methods to use a block cipher to build a cryptographic hash function, specifically a one-way compression function.

The methods resemble the block cipher modes of operation usually used for

Many well-known hash functions, including MD4, MD5, SHA-1 and SHA-2 are built from block-cipher-like components

HMAC can be constructed form the block cipher using cipher block chaining $AES_{c}CBC$ (CBC) mode of operation.

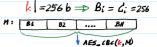
CBC-MAC

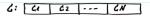
Cipher block chaining message authentication code (CBC-MAC) is a technique for constructing a message authentication code from a block cipher. The message is encrypted with some block cipher algorithm in CBC mode to create a chain of blocks such that each block depends on the proper encryption of the previous block.

This interdependence ensures that a change to any of the plaintext bits will cause the final encrypted block to change in a way that cannot be predicted M - to be signed. $G = AES_{CBC}(k, M)$ encryption of the previous block.

This interdependence ensures that a change to any of the plaintext bits will cause the final encrypted block to change in a way that cannot be predicted or counteracted without knowing the key to the block cipher.

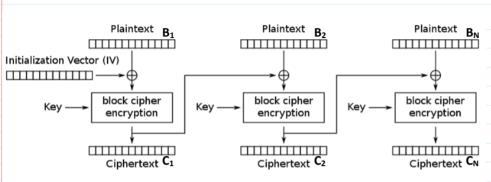
From <https://en.wikipedia.org/wiki/CBC-MAC>





hmac=
$$G_1 \oplus G_2 \oplus ... \oplus G_N = h$$

bituice xoring \int
 $|h| = 256 b$.



Cipher Block Chaining (CBC) mode encryption

Chosep Plaintext Attack

A: